

Church's Reception of Turing's 1936 Paper

a Philosophical Angle

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Turing's Human Computer (*not his analysis*)

(1) behaviorist psychology

(2) & (3) step-by-step account

Turing's Human Computer (*not his analysis*)

- | | | |
|-----------|----------------------------|----------------|
| (1) | behaviorist psychology | [empirical] |
| (2) & (3) | step-by-step account | [mathematical] |
| | (2) propositional language | [non causal] |
| | (3) performative language | [causal] |

Turing's Human Computer (*not his analysis*)

- | | | |
|-----------|----------------------------|----------------|
| (1) | behaviorist psychology | [empirical] |
| (2) & (3) | step-by-step account | [mathematical] |
| | (2) propositional language | [non causal] |
| | (3) performative language | [causal] |

All of this is mathematical for an idealist, i.e., for Turing

Turing's Human Computer (*not his analysis*)

- (1) What human computers accomplish as a result
- (2) & (3) step-by-step account [mathematical]
- (2) propositional language [non causal]
- (3) performative language [causal]

Turing's Human Computer (*not his* analysis)

- (1) What human computers accomplish as a result
- (2) & (3) step-by-step account [mathematical]
- (2) What they *are* doing *when* they compute
- (3) What they *are* supposed (or commanded)
to do *when* they compute

Turing's Human Computer (*not his analysis*)

- (1) What human computers accomplish as a result
- (2) & (3) step-by-step account [mathematical]
- (2) What they *are* doing *when* they compute
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to do *when* they compute

(1) <-> (2) [Schüttpelz 2020, private correspondence]

(1) <-> (3) [Hodges 1983, footnote on p.107]

from Human to Machine (*not his* analysis)

We may now construct a machine to do the work of this computer. To each state of mind of the computer corresponds an “*m*-configuration” of the machine... [Turing 1936, p.251]

Turing ... inconspicuously ... slipped into describing ‘a machine to do the work of this computer’ *in exactly the same language* that was earlier used to characterize the operations of the human computer ... [Schmidt 2011, p.401]

from Human to Machine (*not his analysis*)

[Shanker 1987, p.637]

[Schmidt 2011, p.402]

from Human to Machine (*not his analysis*)

[The] shift from *encoding* to *embodying* marks a categorical departure to causal domains from which there can be no return to normativity

[Shanker 1987, p.637]

... whoever does the calculation understands the rules of the calculus in question

... the calculator has the ability to apply the rules and can justify the procedure and the result with reference to the rules

[Schmidt 2011, p.402]

from Human to Machine (*not his analysis*)

Turing was guilty ... either of

- the illicit assumption that the concept of *following a rule* can be regarded as a **cybernetic mechanism**
- of presenting the steps of a Turing machine program in completely misleading form

[Shanker 1987, p.638]

from Human to Machine (*not his analysis*)

Turing [and computer science at large] are flickering between

- the *normative concept* of following a rule
- the *causal concept* of machinery

Turing

idealism



Schmidt

Shanker

dualism

Turing



Newman



Church

Turing



idealism



dualism



instrumentalism

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Church ... at least until 1937

- Denying the reality of mathematical & logical entities
- Espousing a kind of instrumentalism or fictionalism
- Mathematical entities [Turing's machines] are
 - ❑ fictions,
 - ❑ part of an abstract structure constructed by us to enable us to understand reality



[Anderson 1998, p.137-38]

instrumentalism

Church's 1937 comments

... it shall be possible to devise a computing machine, **occupying a finite space and with working parts of finite size**, which will write down the sequence to any desired number of terms if ...



instrumentalism

Turing



dualism



instrumentalism

Turing



Everything is mathematical



dualism



Nothing is mathematical

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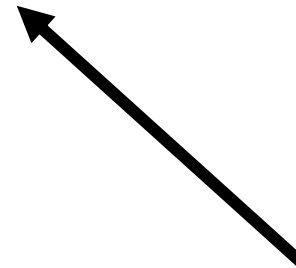
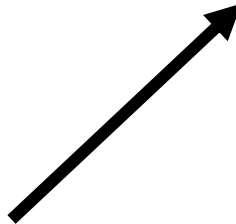
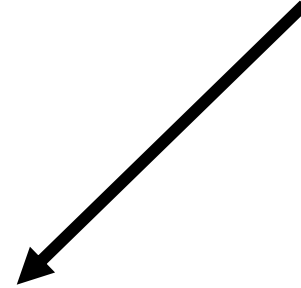
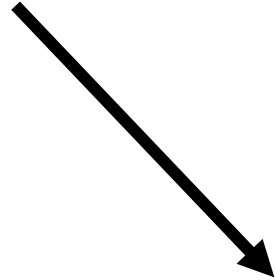
axiom of choice

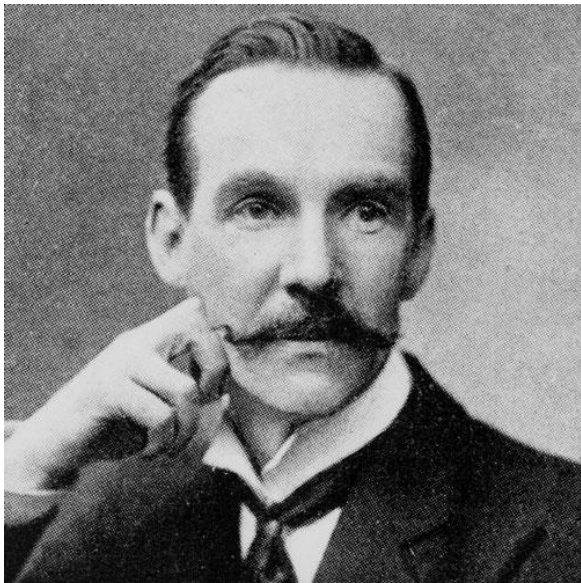
modern physics

Turing 1936

“machine”
metaphor

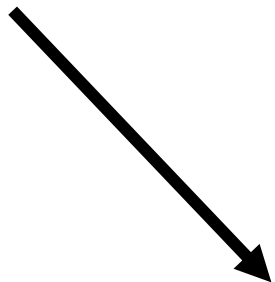
philosophy



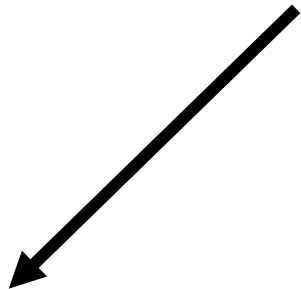


Hobson

of choice

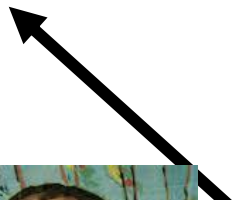
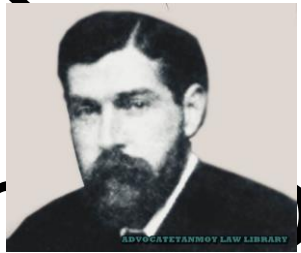
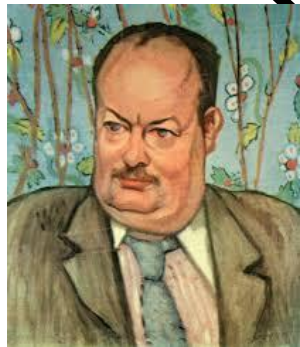
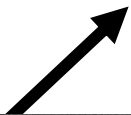


modern



Eddington

Turing 1936

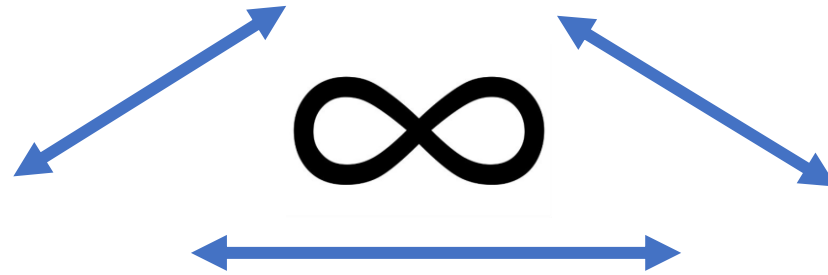




Russell



Hobson



Hardy

Describable in the symbolism of physics?



- Rainbow
- Humour

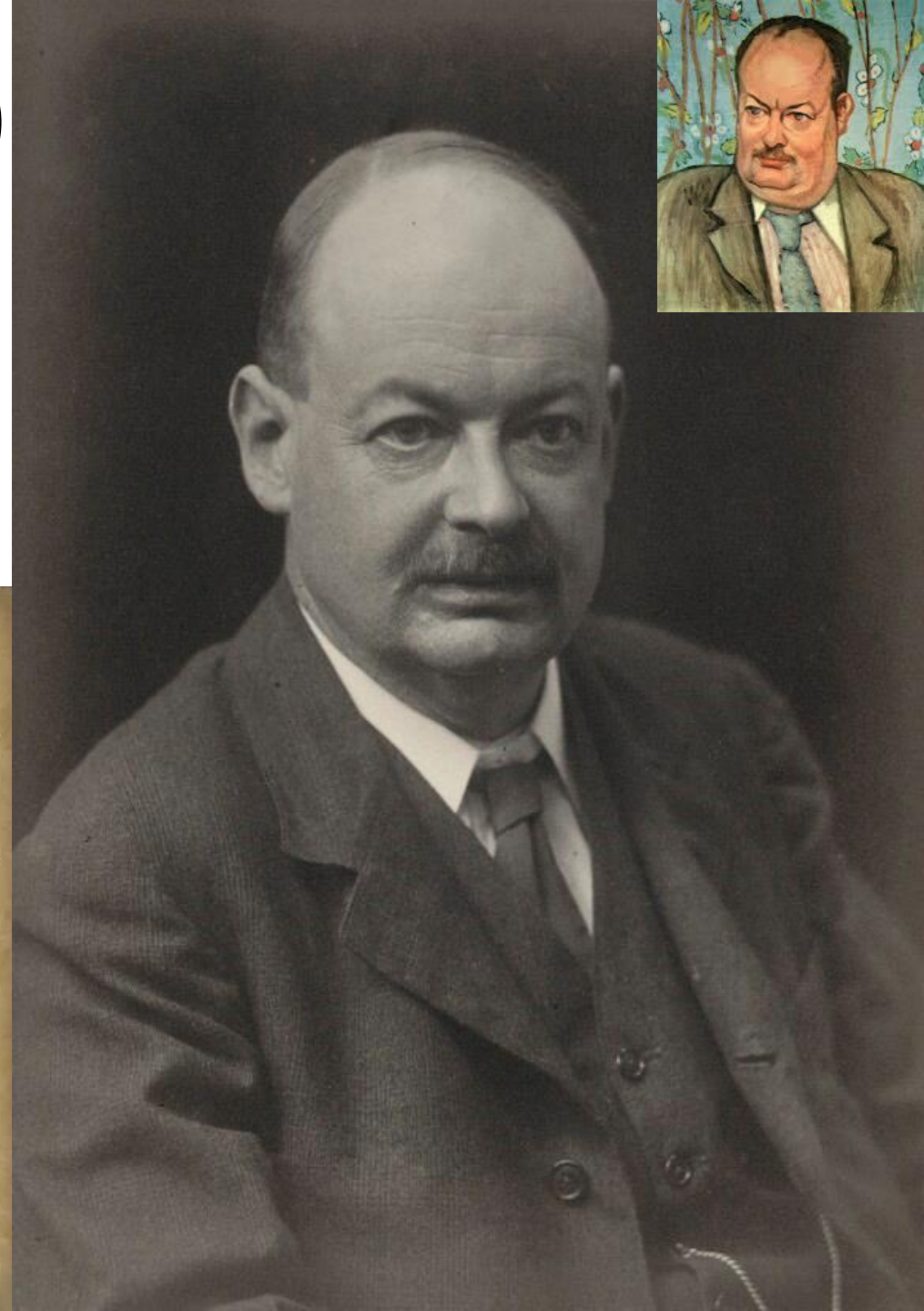
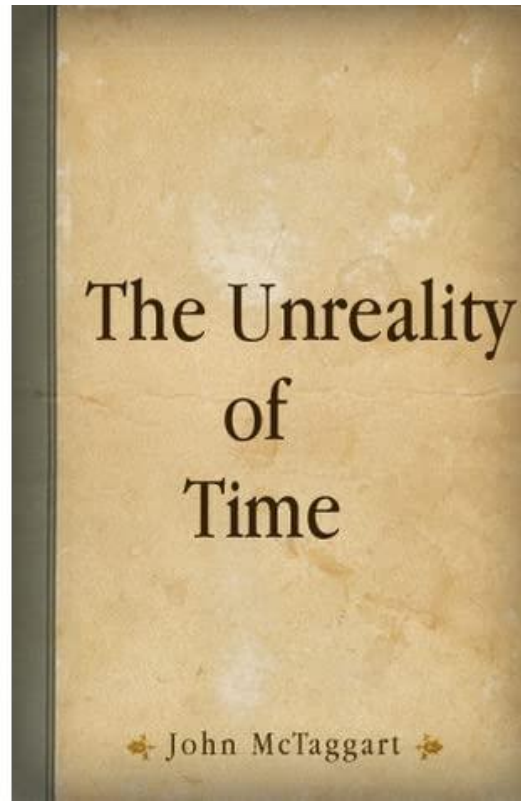
[Eddington 1928, p.322, 328]

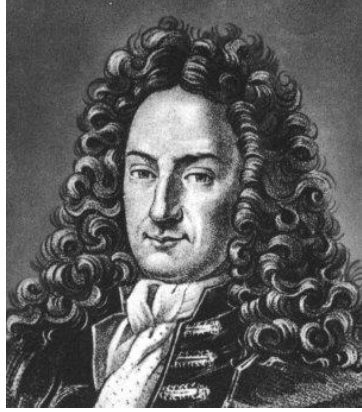
J.M.E. McTaggart (1866-1925)

An *idealist* philosopher in the tradition of

- Hegel
- Bradley

The perception of changing time is an *illusion*





“Souls act according to the laws of final causes, through appetitions, ends, and means.

Bodies act according to the laws of efficient causes or of motions.

And these two kingdoms ... are in **harmony** with each other.”

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Turing did not categorically distinguish
between
a mathematical machine & a physical machine

What, then, did Turing take to be a
`Turing machine' in 1937, in 1948?

Thank you

Bibliography



[Anderson 1998] C. Anthony Anderson, “Alonzo Church’s Contributions to Philosophy and Intensional Logic,” *The Bulletin of Symbolic Logic* 4, no. 2 (1998): 129-171

[Hodges 1983] Andrew Hodges, *Alan Turing: The Enigma* (London: Burnett Books, 1983)

[Schmidt 2011] Kjeld Schmidt, “Dispelling the Mythology of Computational Artifacts,” in *Cooperative Work and Coordinative Practices*, (London: Springer-Verlag, 2011), 391-413

[Shanker 1987] Stuart Shanker, “Wittgenstein versus Turing on the Nature of Church’s Thesis,” *Notre Dame Journal of Formal Logic* 28, no. 4 (1987): 615-649